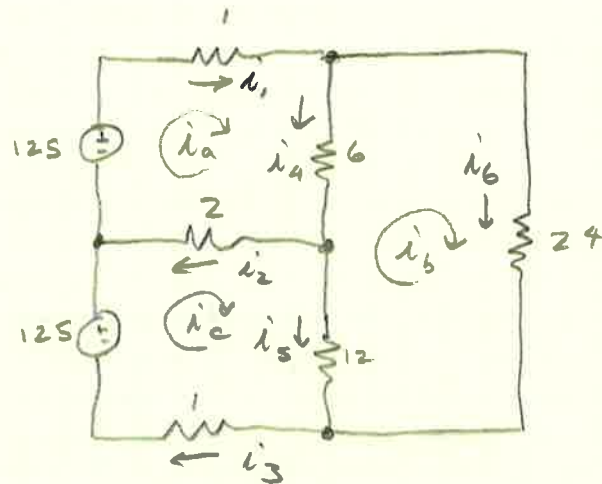


a) Solve for all currents using mesh analysis.



$$i_a: -125 + 1(i_a) + 6(i_a - i_b) + 2(i_a - i_c) = 0$$

$$i_b: 24(i_b) + 12(i_b - i_c) + 6(i_b - i_a) = 0$$

$$i_c: -125 + 2(i_c - i_a) + 12(i_c - i_b) + 1i_c = 0$$

Standard Form:

$$\begin{aligned} 9i_a - 6i_b - 2i_c &= 125 \\ -6i_a + 42i_b - 12i_c &= 0 \\ -2i_a - 12i_b + 15i_c &= 125 \end{aligned}$$

Solving:

$$\begin{aligned} i_a &= 23.76 \text{ A} \\ i_b &= 8.66 \text{ A} \\ i_c &= 18.43 \text{ A} \end{aligned}$$

So

$$\begin{aligned} i_1 &= i_a = 23.76 \text{ A} \\ i_2 &= i_a - i_c = 5.34 \text{ A} \\ i_3 &= i_c = 18.43 \text{ A} \\ i_4 &= i_a - i_b = 15.10 \text{ A} \\ i_5 &= i_c - i_b = 9.77 \text{ A} \\ i_6 &= i_b = 8.66 \text{ A} \end{aligned}$$

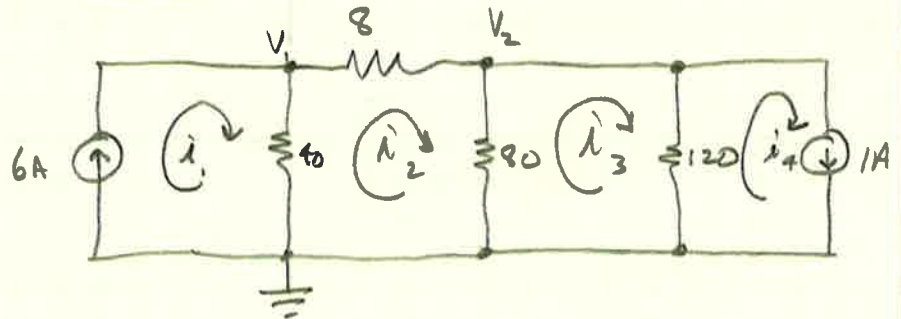
b) Show that Power developed = Power dissipated

$$\begin{aligned} P_{125A} &= (125)(-23.76) = -2970 \text{ W} \\ P_{125B} &= (125)(-18.43) = -2303.75 \text{ W} \end{aligned} \quad \left. \vphantom{\begin{aligned} P_{125A} \\ P_{125B} \end{aligned}} \right\} - 5274 \text{ W}$$

$$\begin{aligned} P_1 &= (23.76)^2 \cdot 1 = 564.54 \text{ W} \\ P_6 &= (15.10)^2 \cdot 6 = 1368.1 \text{ W} \\ P_2 &= (5.34)^2 \cdot 2 = 57.03 \text{ W} \\ P_{12} &= (9.77)^2 \cdot 12 = 1145.4 \text{ W} \\ P_1 &= (18.43)^2 \cdot 1 = 339.7 \text{ W} \\ P_{24} &= (8.66)^2 \cdot 24 = 1800 \text{ W} \end{aligned} \quad \left. \vphantom{\begin{aligned} P_1 \\ P_6 \\ P_2 \\ P_{12} \\ P_1 \\ P_{24} \end{aligned}} \right\} 5275 \text{ W}$$

Find  $v_1$  and  $v_2$  using the mesh current method.

- 1) Pick reference
- 2) assign mesh currents
- 3) solve



$$i_1 = 6A$$

$$\textcircled{1} \text{ mesh } i_2: 40(i_2 - i_1) + 8i_2 + 90(i_2 - i_3) = 0$$

$$\textcircled{2} \text{ mesh } i_3: 90(i_3 - i_2) + 120(i_3 - i_4) = 0$$

$$i_4 = 1A$$

$$\text{Solving } \textcircled{1} + \textcircled{2}: \begin{cases} i_2 = 3A \\ i_3 = 1.8A \end{cases}$$

$$v_1 = 40(i_1 - i_2) = 40(6 - 3) = \underline{\underline{120V}}$$

$$v_2 = v_1 - 8i_2 = \underline{\underline{96V}}$$

a) use mesh-current method to find  $P_{SA}$ .

mesh  $i_1$ :

$$5 + 38(i_1 - i_3) + 30(i_1 + i_2) + 12i_1 = 0$$

mesh  $i_2$ :

$$-67 + 6(i_2 + i_3) + 30(i_2 + i_1) + 40i_2 = 0$$

mesh  $i_3$ :

$$i_3 = 5A$$

Solving:

$$\begin{aligned} i_1 &= 2.5A \\ i_2 &= -0.5A \\ i_3 &= 5A \end{aligned}$$

$$P_{SA} = VI = (V_{38} + V_6) 5A = [38(i_1 - i_3) + 6(i_3 + i_2)] 5 = (-122)(5) = -610W$$

5A source is delivering 610W

b)  $P_{5V} = 5(2.5) = 12.5W$   
 $P_{67} = 0.5(67) = 33.5W$

Total power delivered = 610W

c) check that power delivered = power absorbed

$$\begin{aligned} P_{38} &= (2.5)^2 38 = 237.5W \\ P_6 &= (4.5)^2 6 = 121.5W \\ P_{30} &= (2)^2 30 = 120W \\ P_{40} &= (0.5)^2 40 = 10W \\ P_{12} &= (2.5)^2 12 = 75W \end{aligned}$$

$$\begin{array}{r} +12.5W \\ +33.5W \\ \hline 610W \end{array}$$

✓

